

# PHYSICS-DYNAMICS INTERFACE

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# Plan of the lecture

- Physics in the NWP model – the notion of parameterizations and concepts;
- Flux form formulation – property of conservation;
- Basic hypothesis and system of equations for moist physics;
- Example of the realization – thermodynamic basis for the ALARO microphysics;
- Link to the deep moist convection parameterization

# What are parameterisations, how to define their ensemble? (1/3)

- Two *open* limits: with *the resolved dynamics* and with the *yet too sophisticated processes* => no single definition.
- Traps:
  - wrong perception of cause and consequence;
  - wrong perception of model-dependency;
  - lost search for super-conservative variables.
- Misleading definitions:
  - terms treated in a ‘statistical’ sense;
  - non-linear terms;
  - balance with dynamical tendencies (‘on demand’ parameterisation misleading dream).

# What are parameterisations, how to define their ensemble? (2/3)

- Diabaticism (non conservation of energy, angular momentum or moisture in the Lagrangian sense)
  - but which energy (example of latent heat)?
  - some purely adiabatic effects must be parametrised (e.g. impact of stagnant cold air on the upper flow).
- Irreversibility (no correct back-integration in time)
  - some phenomenon are reversible at one scale and irreversible at another one.
  - difficult partition (e.g. condensation vs. precipitation).
- Sub-grid scale choice
  - radiation and phase changes are basically grid-scale;
  - surface forcing is always sub-grid-scale.

# What are parameterisations, how to define their ensemble? (3/3)

- A practical way out of all these vicious circles:
  - have a global look at the ***cycles***;
  - search conservation laws (Green-Ostrogradsky trick);
  - treat and discretise “unknown terms” on a case to case basis:
    - statistical approach for purely non-linear problems;
    - complex algorithmic for phase changes;
    - attention focused on feed-back loops;
    - numerical analysis for irreversibility, stiffness and non-linear instability;
    - avoid the problem of parameterisation (or modelling) inside the parameterisation.
- Ultimately, verify scale-independency as well as consistency (even after discretisation).
- A parameterization is intended to produce correctly the average impact of the process within each grid-box.

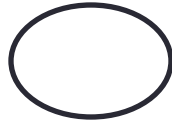
# Processes treated in NWP models (most frequently parameterized ones)

- Turbulent fluxes (between the surface and the lowest model level and between two model levels);
  - Orographic mountain drag/lift;
  - Soil processes;
  - Cloudiness;
  - Stratiform (grid-box scale) precipitation;
  - Convection (moist deep; i.e. with precipitation);
  - Radiation
- 
- Parameterization schemes generate tendencies, which impact the dynamical core variables (pressure, temperature, wind) and other prognostic variables (moisture species, TKE, ...)

# Interactions and feed-back loops



= quantities



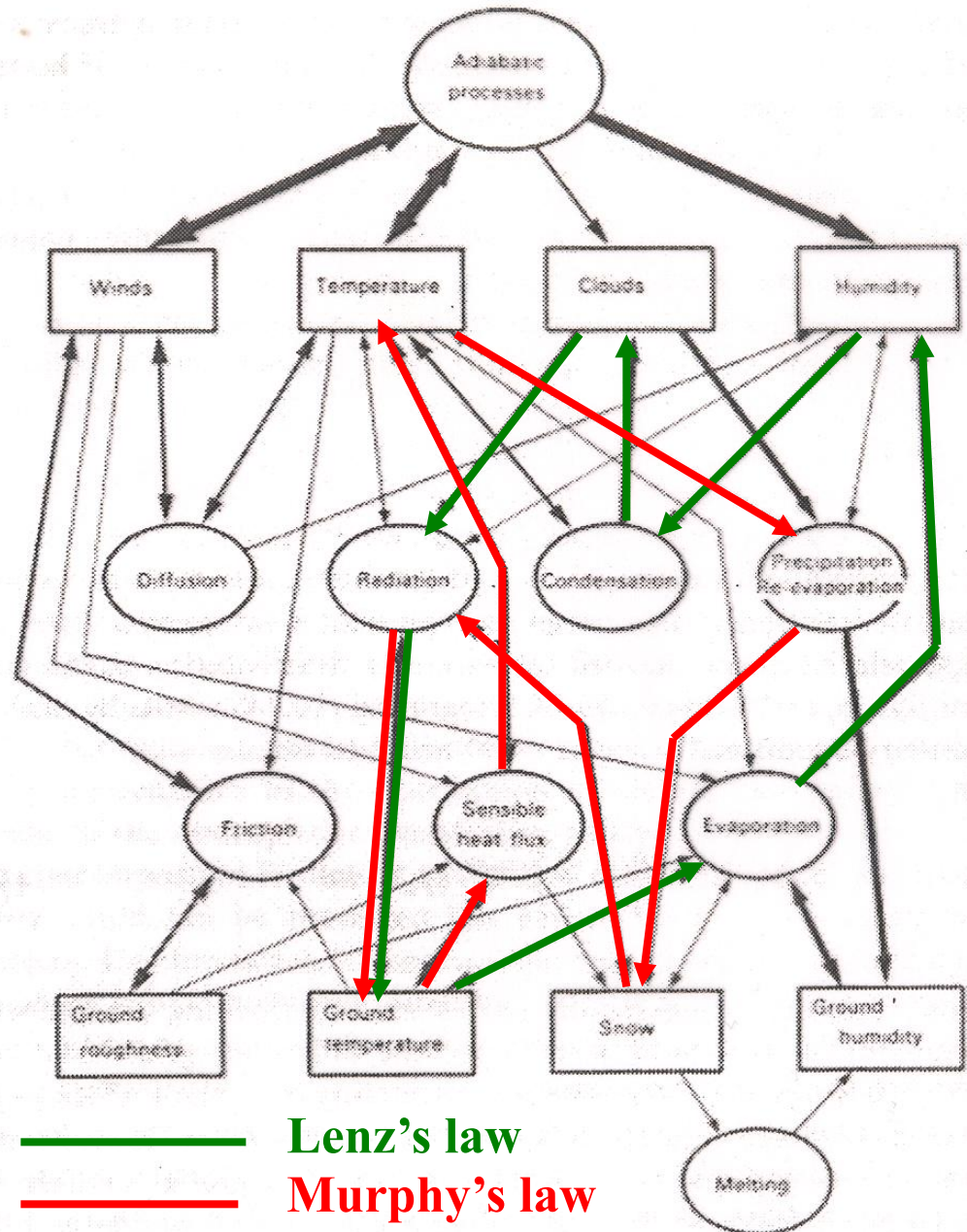
= processes

→ = impact or control

*Every closed loop of arrows represent a feed-back process*

*Negative feed-back loop, the effect counteracts the cause*

*Positive feed-back loop, the effect amplifies the cause*



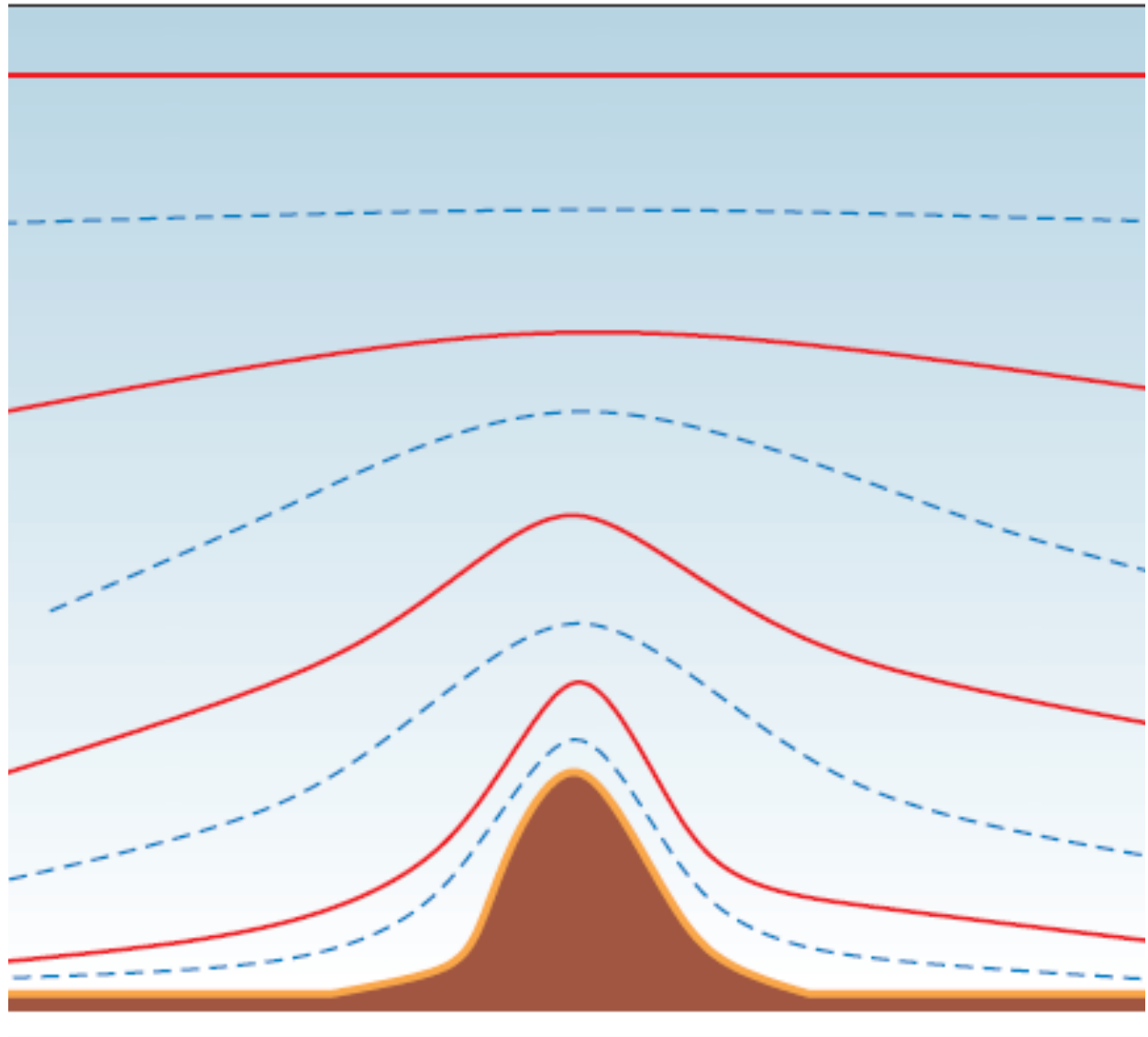
## Flux form to treat the physics tendencies

In NWP the physics is 1D – we treat the vertical column.

Given the respective horizontal and vertical resolution ratios, grid-boxes are still very flat – together with the nature of the processes it gives a good justification to work with the vertical fluxes.

Fluxes are defined at the layer interfaces – red lines. Their divergence gives the tendency in the layer – dashed blue lines.

Conservation is ensured.





# Flux form interfacing (1/2)

- Flux transport, on the basis of the equations

$$\frac{(\quad)}{t} = g \cdot \frac{(F)}{p} \quad F = \overline{\quad} \cdot w \cdot$$

- Examples

- Energy  $(\quad) = \frac{J}{kg} \quad (F) = \frac{kg}{m^3} \cdot \frac{m}{s} \cdot \frac{J}{kg} = \frac{J}{m^2 \cdot s} = \frac{W}{m^2}$

- Species  $(\quad) = [1] \quad (F) = \frac{kg}{m^3} \cdot \frac{m}{s} \cdot [1] = \frac{kg}{m^2 \cdot s}$

- Momentum

$$(\quad) = \frac{m}{s} \quad (F) = \frac{kg}{m^3} \cdot \frac{m}{s} \cdot \frac{m}{s} = \frac{kg}{m \cdot s^2} = [Pa] !!$$

# Flux form interfacing (2/2)

- Energy conversion, example of potential to kinetic

- Locally

$$\frac{R \cdot T}{p} = \frac{J}{kg \cdot K} \cdot \frac{Pa}{s} \cdot \frac{K}{Pa} = \frac{W}{kg}$$

- Integrally

$$\frac{R \cdot T}{p} \cdot \frac{dp}{g} = \frac{W}{kg} \cdot \frac{kg}{m^2} = \frac{W}{m^2}$$

Vertical integrand

of course !

Green-Ostrogradsky

# Simplifying hypothesis (1/3)

- In order to get the **governing *diabatic* equations**, i.e. including the source terms from the physics, we need to apply some simplifying hypothesis.
- Here the goal is to obtain a set of consistent simplifications in order to have a useful view of the **atmospheric thermodynamics**.
- ‘Useful’ means here:
  - Can be converted into tractable equations;
  - Can give a conservative view of the conversions (Green-Ostrogradsky again);
  - Can be put in relation with existing measurements.

# Simplifying hypothesis (2/3)

Main hypotheses:

- **How the atmospheric mass vary with the hydrological cycle:**
  1. **Conservation of the total mass:** all types of precipitation leaving the atmosphere have a counter-flux of dry air. Prevailing choice in NWP.
  2. **Mass changes are controlled by the precipitation-evaporation budget at the surface.** There is no compensation by dry air. This option has consequences on the continuity equation => pressure tendency and vertical velocity depend on the surface precipitation flux.
- **All gases obey Boyle-Mariotte's and Dalton's laws**  
=> state equation is tractable.
- **Condensed phases have a zero volume**  
=> avoids the non-compressibility problem for associated portion of the atmospheric content.

# Simplifying hypothesis (3/3)

- All specific heat values are temperature independent
  - => linear dependency of latent heats on temperature. Clausius-Clapeyron equation can be analytically integrated and yield rather accurate values of saturation pressures
- Atmosphere is in permanent thermodynamic equilibrium
  - => derivation of enthalpy budgets, flux-divergence form of tendencies;

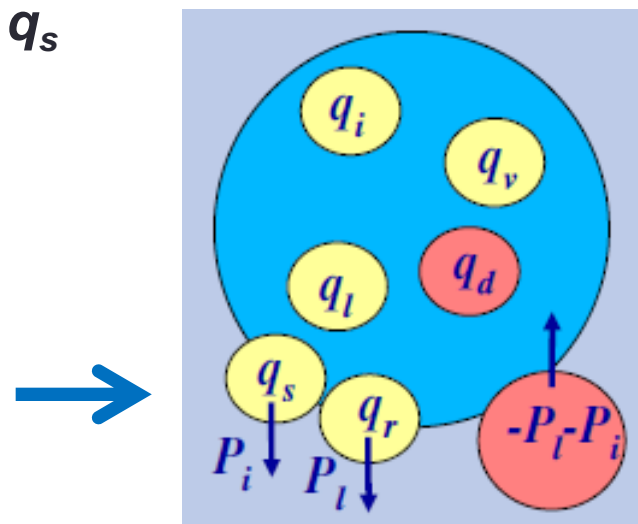
# Link to a microphysical scheme

- Considered species:

1. Dry air:  $q_d$
2. Water vapour:  $q_v$
3. Cloud (suspended) liquid water:  $q_l$
4. Cloud (suspended) ice:  $q_i$
5. Rain (falling precipitation):  $q_r$
6. Snow (any solid falling precipitation):  $q_s$

$$q_d + q_v + q_l + q_i + q_r + q_s = 1$$

We shall retain the option of conserving the total mass of the atmosphere



# Thermodynamic basis for equations

All phase changes pass by vapor phase – thermodynamically equivalent and easy budget interface.

Graupel and hail can be treated as sub-classes of snow.

## Pseudo- fluxes:

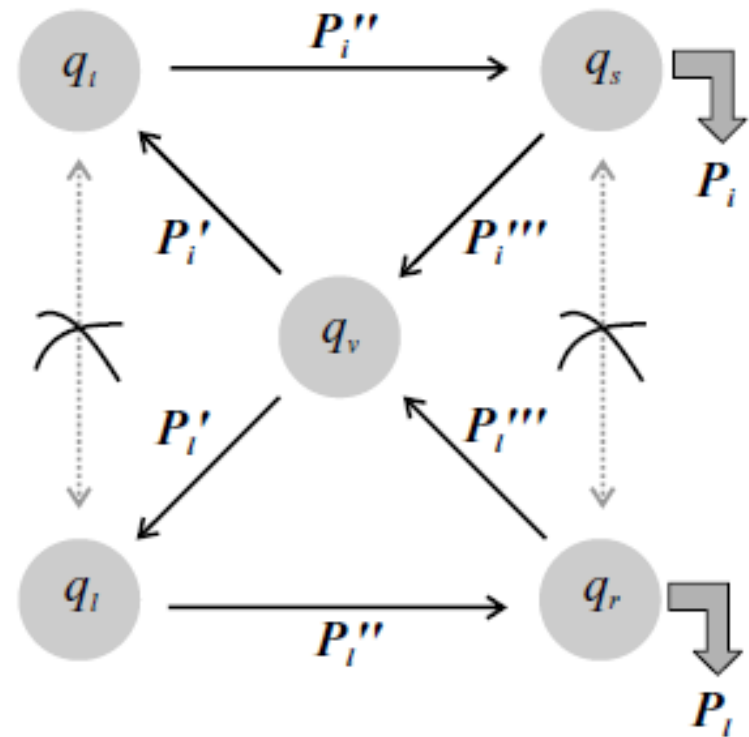
Condensation  $P'_{(l/i)}$

Autoconversion  $P''_{(l/i)}$

Evaporation  $P'''_{(l/i)}$

## Precipitation fluxes:

Liquid and solid:  $P_{(l/i)}$



# Evolution of temperature – enthalpy budget

$$\frac{\partial}{\partial t}(c_p T) = -g \frac{\partial}{\partial p} \left[ \begin{array}{c} (c_l - c_{pd})P_l T + (c_i - c_{pd})P_i T \\ -(\hat{c} - c_{pd})(P_l + P_i)T \\ +J_s + J_{rad} \\ -L_l(T_0)(P'_l - P'''_l) - L_i(T_0)(P'_i - P'''_i) \end{array} \right]$$

$$c_p = c_{pd}q_d + c_{pv}q_v + c_l(q_l + q_r) + c_i(q_i + q_s)$$

$$\hat{c} = \frac{c_{pd}q_d + c_{pv}q_v + c_lq_l + c_iq_i}{1 - q_r - q_s}$$

$$L_{l/i}(T) = L_{l/i}(T_0) + (c_{pv} - c_{l/i})T$$

Derivation is based on entropy equation, here is the compact result.

The sum of all terms in the bracket above gives the total enthalpy flux.

**Red term** exists in fully mass weighted framework only.



# Evolution of species

$$\frac{dq_v}{dt} = g \frac{\partial}{\partial p} \left[ P_l'''' + P_i'''' - P_l' - P_i' + \frac{q_v(P_l + P_i)}{1 - q_r - q_s} - J_{q_v} \right]$$

$$\frac{dq_l}{dt} = g \frac{\partial}{\partial p} \left[ P_l' - P_l'' + \frac{q_l(P_l + P_i)}{1 - q_r - q_s} - J_{q_l} \right]$$

$$\frac{dq_i}{dt} = g \frac{\partial}{\partial p} \left[ P_i' - P_i'' + \frac{q_i(P_l + P_i)}{1 - q_r - q_s} - J_{q_i} \right]$$

$$\frac{dq_r}{dt} = g \frac{\partial}{\partial p} [P_l'' - P_l'''' - P_l]$$

$$\frac{dq_s}{dt} = g \frac{\partial}{\partial p} [P_i'' - P_i'''' - P_i]$$

Derivation is based on the conservation.

**Red terms** exists in fully mass weighted framework only.

# Further requirements on the microphysics scheme (ALARO example)

Challenges to construct the microphysics for NWP:

- Use of **flux-conservative thermodynamic equations** and well defined interface;
- Possibility of using relatively long time-steps (numerics and sedimentation problem => **statistical sedimentation**);
- Possibility of **unified treatment for stratiform and convective clouds** (sub-grid-scale geometry of clouds and precipitation) – Grey zone challenge of moist deep convection but not only;
- **Modularity** (ready to test options in the same environment otherwise).

# Sub-grid geometry of clouds and precipitation



# As conclusion for Lesson

***Probably more than 90% of erroneous scientific statements about the modelled behaviour of the atmosphere come from methodological errors!***