



**Lomonosov Moscow State University**  
Faculty of geography  
Department of meteorology and climatology



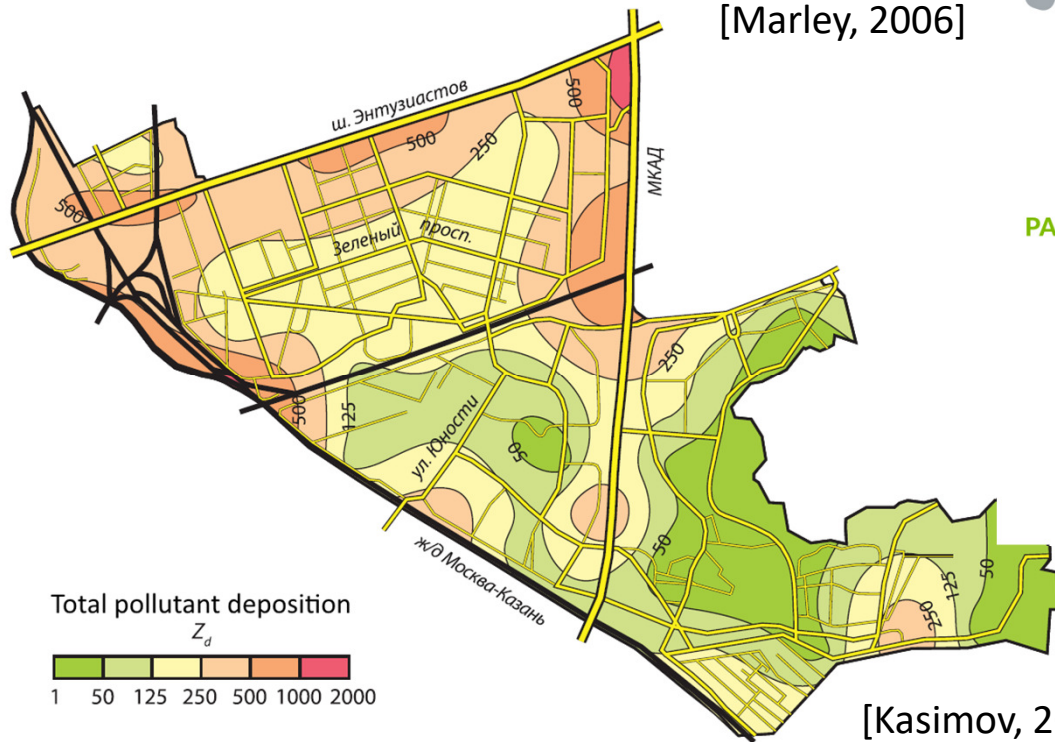
# Simulation of particle transport in urban environments with high spatial resolution

Alexander Varentsov, Viktor Stepanenko, Pavel Konstantinov

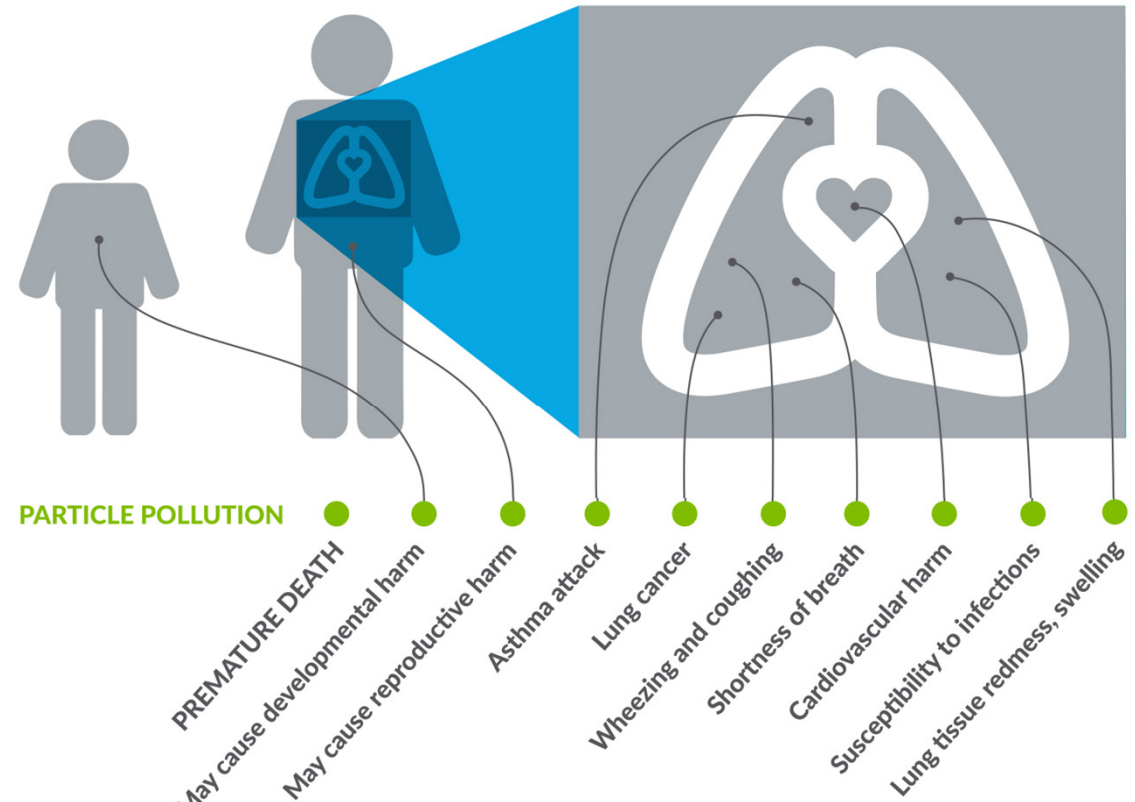
# Motivation: atmospheric aerosol

Particle size	Impact area
5 – 30 $\mu\text{m}$	Nose, Throat, Mouth
1 – 5 $\mu\text{m}$	Trachea, upper bronchi
< 1 $\mu\text{m}$	Lungs, circulatory system

[Marley, 2006]



[Kasimov, 2016]



[<https://www.lung.org>]

# Objective

**Objective:** development of lagrangian tool for calculating aerosol dispersion in urban geometry with high spatial resolution

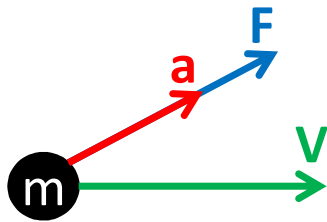
**Tasks:**

- Development of physical model of particle advection
- Implementation of the scheme in the program code
- Testing the model for idealized cases and real urban built-up areas

# Particle Advection Physics

Newton's second law

$$m\mathbf{a} = m \frac{d\mathbf{v}}{dt} = \mathbf{F}$$



Medium resistance force

$$F_D = \frac{3\mu C_D Re}{4\rho_p d_p^2}$$

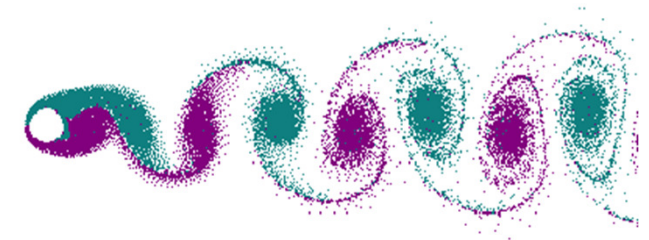
Motion equation

$$\frac{d\mathbf{u}_p}{dt} = \frac{\mathbf{g}(\rho_p - \rho)}{\rho_p} + F_D(\mathbf{u} - \mathbf{u}_p)$$

The equation is solved by 4-order explicit Runge-Kutta method

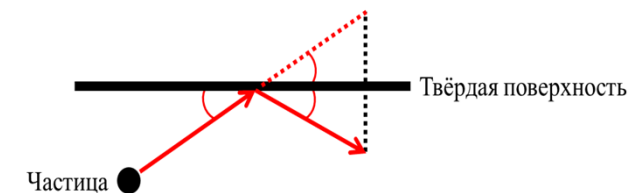
Trajectory calculation is possible for a variety of particles.

Turbulent eddies



[<http://www.mcef.ep.usp.br>]

Interaction with surfaces



$C_D$  – drag coefficient  
 $Re$  – Reynolds number

$\rho_p$  – particle density  
 $d_p$  – particle diameter  
 $\mathbf{u}_p$  – particle velocity

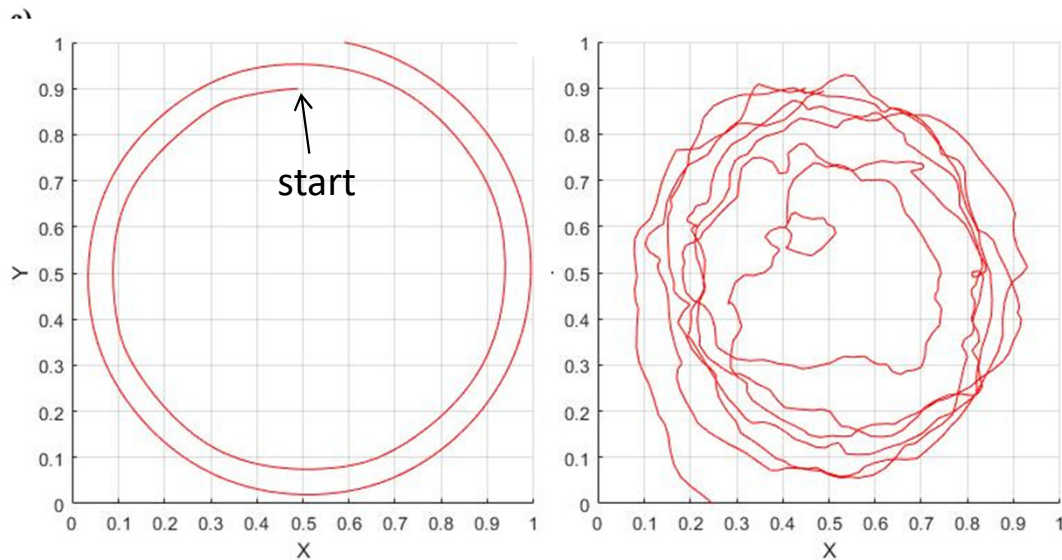
$\rho$  – medium (air) density  
 $\mathbf{u}$  – flow velocity

# Testing for idealized flow

Circular flow  $\mathbf{u} = \boldsymbol{\Omega} \times \mathbf{r}$

Laminar flow

Turbulent flow



$\boldsymbol{\Omega} = (0,0,1)$   
 $\mathbf{r}$  – position vector

## Turbulence Parameterization

Flow velocity  $\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}'$   
 $\mathbf{u}'$  – pulsation component  
(normally distributed random variable)

Discrete random walk  
model

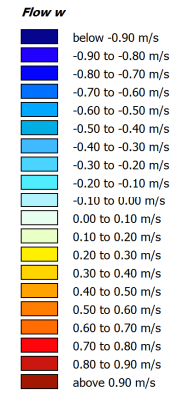
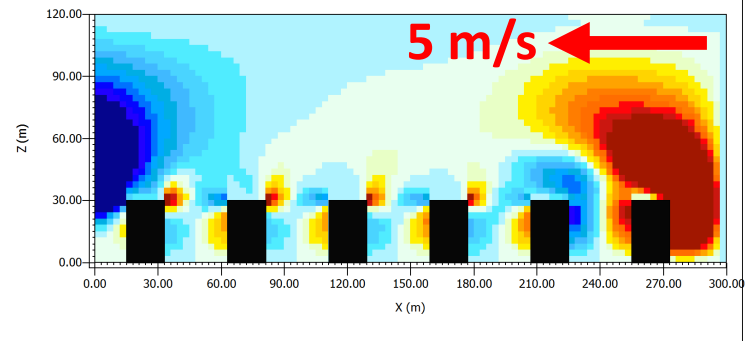
$\mathbf{u}'$  is generated for every large turbulent eddy

$$\tau = \min(t_e, t_R)$$

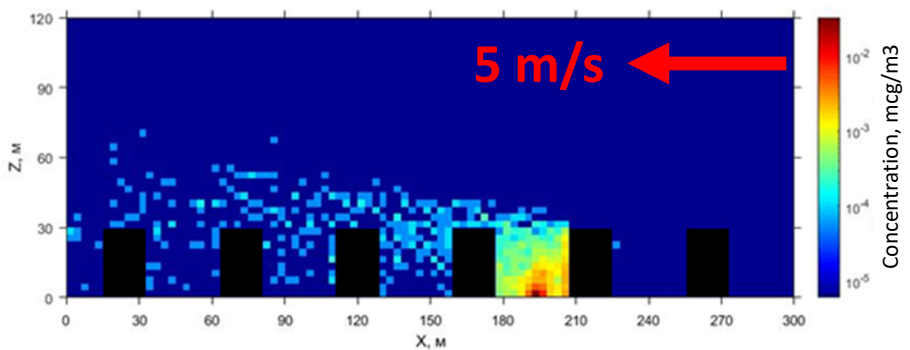
$t_e$  – eddy lifetime  
 $t_R$  – eddy crossing time

# Urban canyon case

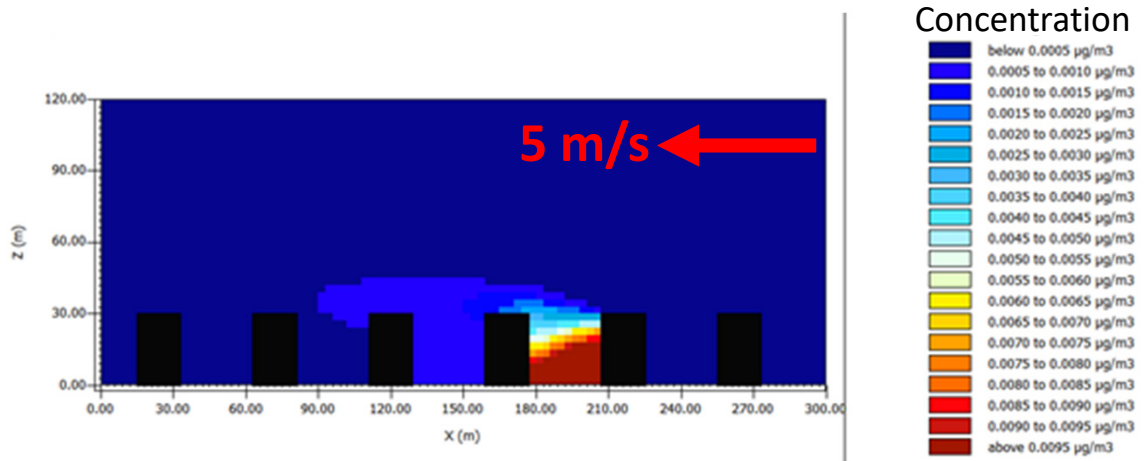
Flow vertical velocity



Developed model (lagrangian)



ENVI\_MET model (eulerian)



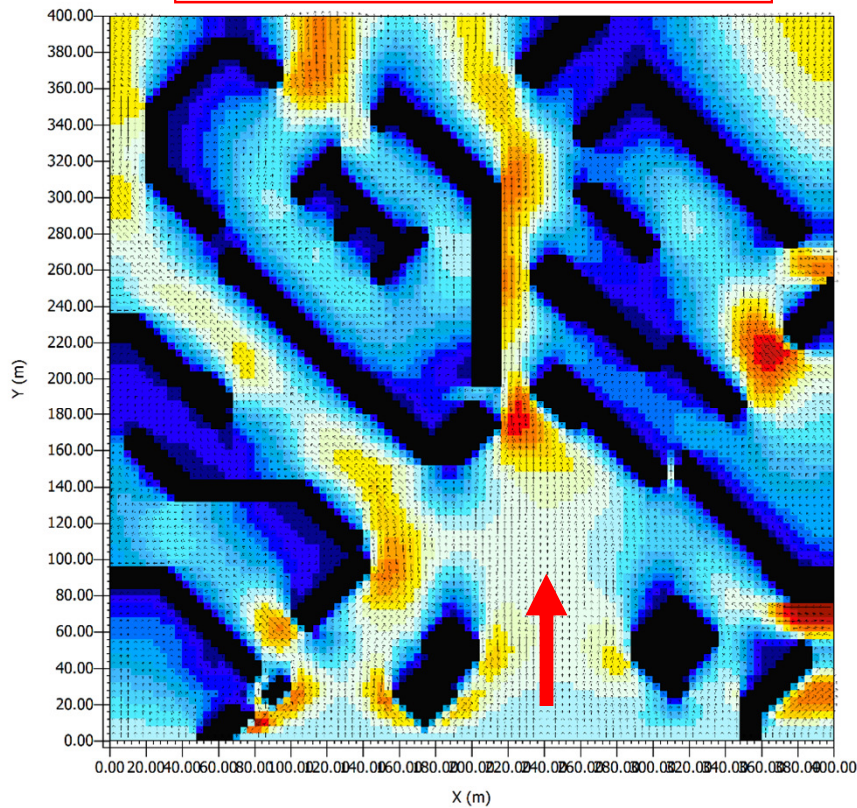


# Close to real conditions Nadya city case

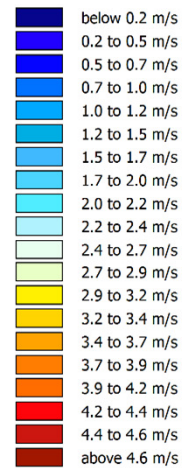
Nadya, 400x400 m

Flow velocity on 10m – 5 m/s

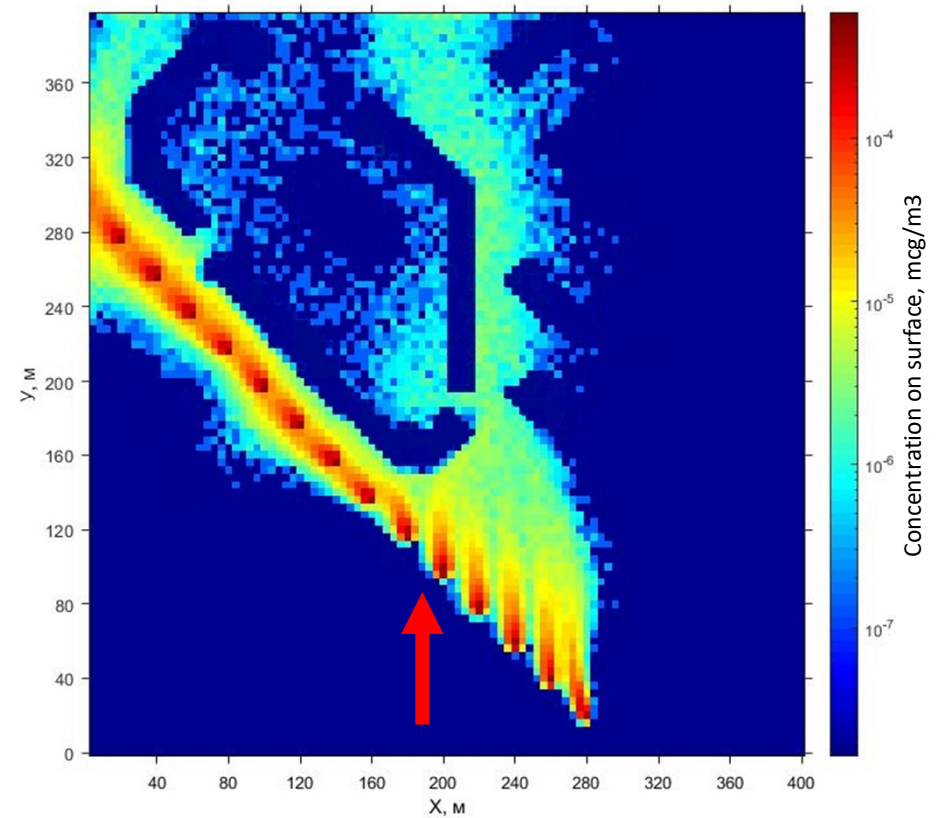
1.2m level wind velocity



Wind velocity on  
1.2m level, m/s



PM2.5 concentration on surface

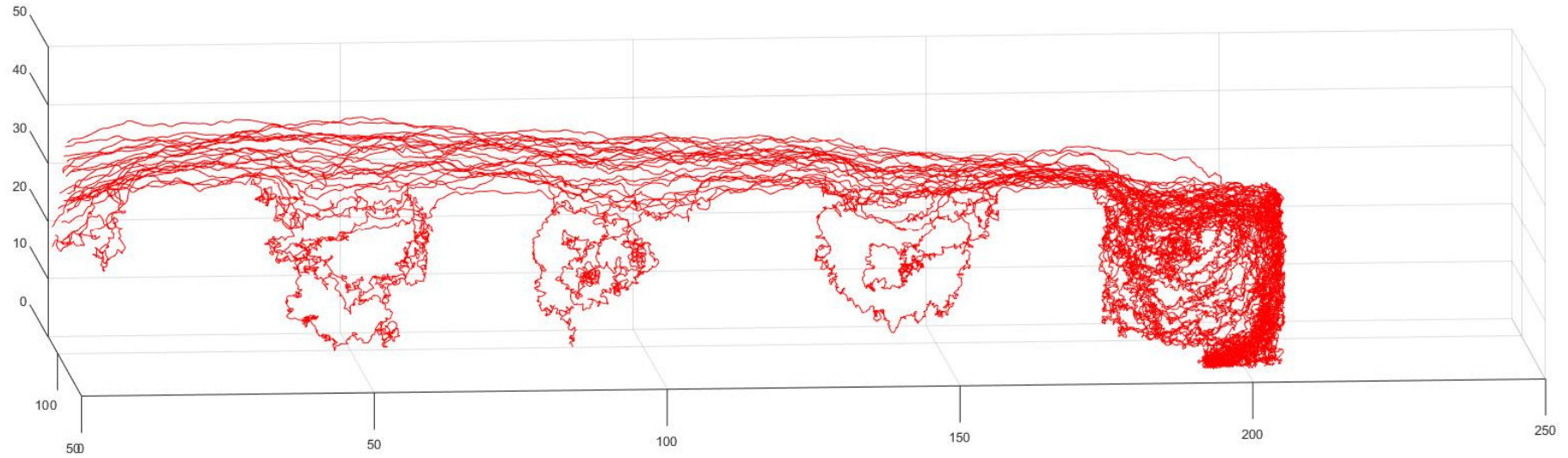


# Conclusions

- **The 3D microscale Lagrangian model of particle advection was developed and implemented in the program code**
- The model has ability to calculate the particle dispersion in advanced geometry of urban areas and to accept various types of input data. In perspective this tool could be more accurate, than eulerian method
- Simple analytical and close to real conditions tests were successfully carried out



# Thank you for attention!

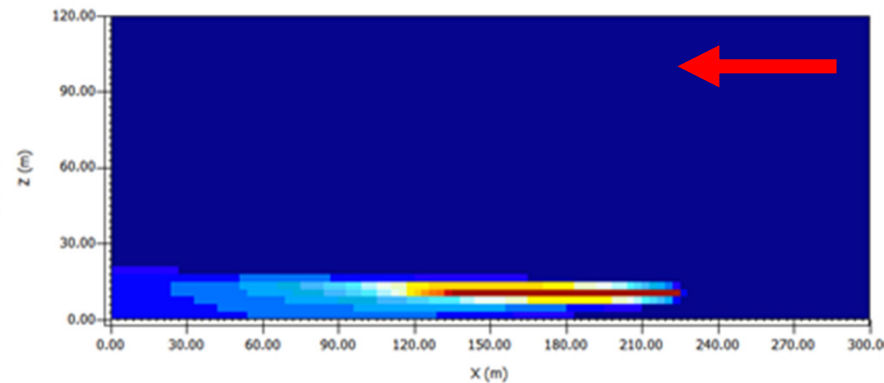
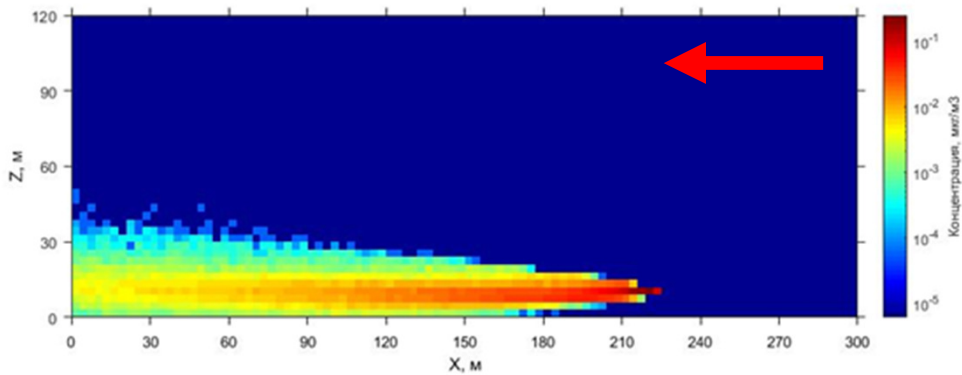


# Flat surface: concentration

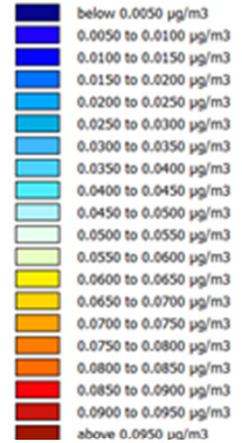
Developed model (lagrangian)

ENVI\_MET model (eulerian)

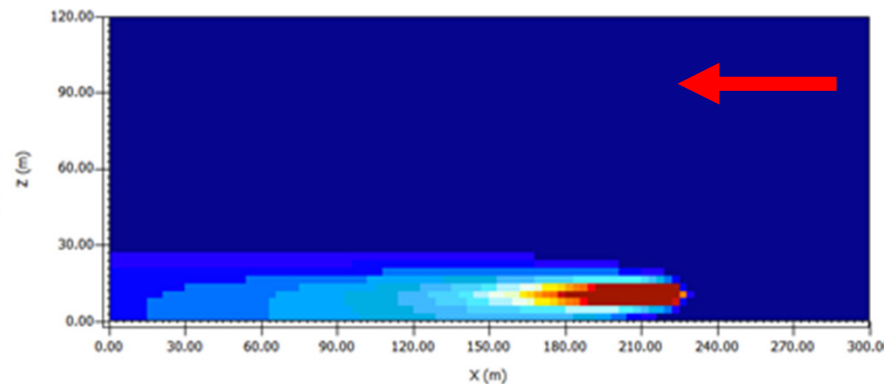
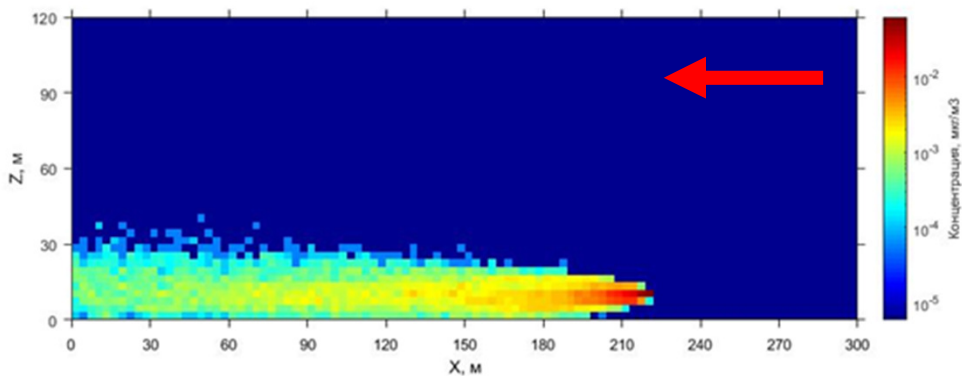
Flow velocity on 10m – 0.5 m/s



Concentration



Flow velocity on 10m – 5 m/s



Concentration

